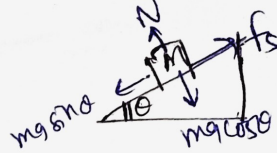


Friction



- ① $F_a =$ applied force
- $F_{smax} = \mu_s N$ (Limiting condⁿ)
- $F_k = \mu_k N$

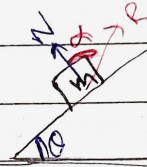
① angle of inclined plane < angle of Repose
- static friction.

$F_s = mg \sin \theta$ $\tan \theta < \mu_s$

② Real area = 10^{-4} x virtual area

② angle of inclined plane > angle of Repose

③ $F_{pulling} = \frac{\mu_s Mg}{(\cos \theta + \mu_s \sin \theta)}$



$\tan \theta > \mu_s$

$F_k = \mu_k mg \cos \theta$

④ $F_{pushing} = \frac{\mu_s Mg}{(\cos \theta - \mu_s \sin \theta)}$
 $\tan \theta = \mu_s$

$mg \sin \theta - \mu_k mg \cos \theta = Ma$
 $\alpha = 0$

$F_{pulling} < F_{pushing}$

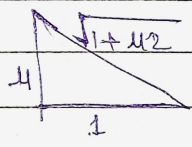
⑤ Two inclined planes (one is smooth and other is rough).

⑥ special case (only pulling force)

⑦ At what angle pulling force must be applied, such that its value is minimum?

$\mu = \frac{(n^2 - 1) \tan \theta}{n^2}$

$\tan \theta = \mu_s$



max. and min. forces

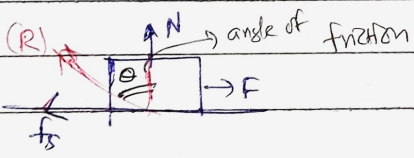
$F_{min} = \frac{\mu Mg}{\sqrt{1 + \mu^2}}$
 $\rightarrow \tan \theta$

① inclined at 45°

$F_{min} \leq F \leq F_{max}$

$mg(\sin \theta - \mu \cos \theta) \leq F \leq mg(\sin \theta + \mu \cos \theta)$

⑧ Resultant mu force (R)

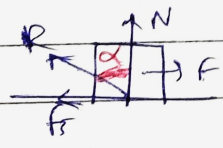


② Force is applied \perp to ground

$F_{min} \leq F_{\perp to ground} \leq F_{max}$

$mg(\sin \theta - \mu \cos \theta) \leq F_{\perp to ground} \leq mg(\sin \theta + \mu \cos \theta)$
 $(\cos \theta + \mu \sin \theta)$ $(\cos \theta - \mu \sin \theta)$

⑨ angle of friction (α)



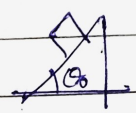
⑩ Force \perp to inclined plane.

$F_{max} = \infty$ such

$F_{min} = \frac{mg(\sin \theta - \mu \cos \theta)}{\mu}$

⑪ Angle of Repose.

$\tan \theta_0 = \mu_s$



$$a_{f2} = a_{f1}$$

(10) Truck box problem

a) Horizontal truck box

$$a_0 = \mu g \quad \text{--- limiting cond}^n$$

① $a_{truck} < \mu g (a_0)$

$$f_s = f_{applied} = Ma_T$$

② $a_{truck} > \mu g (a_0)$

$$Ma_T - \mu k Mg = Ma_{rel}$$

③

time after which block flow off truck

$$s = \frac{1}{2} a_{rel} t^2$$

$$v^2 = u^2 - 2a_{truck} s$$

$$\therefore t = \sqrt{\frac{2l}{a_{rel}}}$$

b) Vertical truck-box problem

$$a_0 = \frac{g}{\mu} \quad \text{--- limiting cond}^n$$

① $a_{truck} > g/\mu$

$$f_{static} = Mg$$

② $a_{truck} < g/\mu$

$$Ma_{rel} = mg - \mu k a_T$$

(11) Block on block problem

steps ① $f_{s1, max}$ & $f_{s2, max}$ $a_{1,0}$ & $a_{2,0}$ $a_{1,0}$ & $a_{2,0}$ $a_{1,0}$ & $a_{2,0}$ resp.

② system boundary or Acceleration $a_{1,0}$ & $a_{2,0}$

③ $f_{s, max}$ $a_{1,0}$ value A $a_{1,0}$ regarding $a_{1,0}$ $f_{s, max}$ still compare $a_{1,0}$ $a_{1,0}$ $a_{1,0}$ $a_{1,0}$ $a_{1,0}$ both blocks will move separately,

④ and after all these, a_1 & a_2 $a_{1,0}$ & $a_{2,0}$

(12) Block against vertical wall

--- same concept like vertical truck-box problem

$$a = \frac{g}{\mu}$$

(12) chain on horizontal table

$$x = \frac{\mu}{(\mu+1)} L$$

x = hanging chain's length

L = length of chain